

2003 Canadian Computing Competition, Stage 2  
Day 2, Question 1

Input file: perm.in  
Output file: perm.out  
Source file: n:\perm\perm.\_\_\_\_

### Constrained Permutations

A *permutation* on the numbers  $1, 2, \dots, n$  is a linear ordering of the numbers. For example, there are 6 permutations of the numbers 1,2,3. They are 123, 132, 213, 231, 312 and 321. Another way to think of it is removing  $n$  disks numbered 1 to  $n$  from a bag (without replacement) and recording the order in which they were drawn out.

Mathematicians (and other smart people) write down that there are  $n! = n \cdot (n-1) \cdots 3 \cdot 2 \cdot 1$  permutations of the numbers  $1, \dots, n$ . We call this “ $n$  factorial.”

For this problem, you will be given an integer  $n$  ( $1 \leq n \leq 9$ ) and a series of  $k$  ( $k \geq 0$ ) constraints on the ordering of the numbers. That is, you will be given  $k$  pairs  $(x, y)$  indicating that  $x$  must come before  $y$  in the permutation.

You are to output the number of permutations which satisfy all constraints.

#### Input

Your input will be  $k + 2$  lines. The first line will contain the integer  $n$ . The second line will contain the integer  $k$ , indicating the number of constraints. The remaining  $k$  lines will be pairs of distinct integers which are in the range  $1, \dots, n$ .

#### Output

Your output will be one integer, indicating the number of permutations of  $1, \dots, n$  which satisfy the  $k$  constraints.

#### Sample Input 1

```
3
2
1 2
2 3
```

#### Sample Output 1

```
1
```

**Sample Input 2**

4  
2  
1 2  
2 1

**Sample Output 2**

0

**Sample Input 3**

4  
2  
1 2  
2 3

**Sample Output 3**

4