

## Problem of the Week

### Problem C and Solution

### Garden Paths

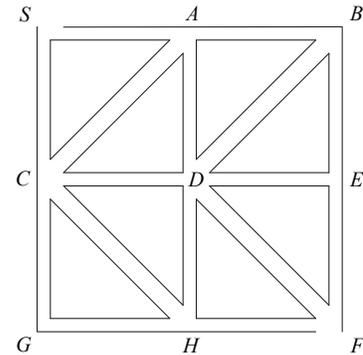
#### Problem

In a garden, Jazzmin travels through the labyrinth shown above from Entrance to Exit. She is only allowed to travel east, south, or southeast along a path. How many different routes can Jazzmin take from Entrance to Exit?

#### Solution

We could solve this problem by tracing out different routes and counting how many we find. We will set up a systematic approach to doing so, to ensure that we do not miss any routes.

We begin by labelling the Entrance with the letter  $S$  for Start and the Exit with the letter  $F$  for Finish. We will then label the seven intersections in the maze as  $A, B, C, D, E, G,$  and  $H,$  as shown.



Since Jazzmin can only travel east, south, or southeast along a path, starting at  $S$  she has only two choices as to where to go next:  $A$  or  $C$ .

#### Case 1: Jazzmin travels from $S$ to $A$

Again, since Jazzmin can only travel east, south, or southeast along a path, she has only two choices as to where to go next:  $B$  or  $D$ .

If Jazzmin travels to  $B$ , then since she can only travel east, south or southeast, she must go to  $E$  next, followed by  $F$ . Therefore, one route from  $S$  to  $F$  is  $SABEF$ .

If Jazzmin travels to  $D$ , then since she can travel east, south or southeast, she can go to  $E$ ,  $F$  or  $H$  next.

- If she travels from  $D$  to  $E$ , she must then go to  $F$ . Therefore, one route from  $S$  to  $F$  is  $SADEF$ .
- If she travels from  $D$  to  $F$ , we have found another route. Therefore, one route from  $S$  to  $F$  is  $SADF$ .
- If she travels from  $D$  to  $H$ , she must then go to  $F$ . Therefore, one route from  $S$  to  $F$  is  $SADHF$ .

Therefore, there are four routes from  $S$  to  $F$  in which Jazzmin first travels from  $S$  to  $A$ . They are  $SABEF$ ,  $SADEF$ ,  $SADF$ , and  $SADHF$ .





**Case 2:** Jazzmin travels from  $S$  to  $C$

Since Jazzmin can travel east, south or southeast, she could travel to  $D$ ,  $H$  or  $G$  next.

- If she travels from  $C$  to  $D$ , she again has 3 choices: travel from  $D$  to  $E$ ,  $F$  or  $H$ . We get three different routes:  $SCDEF$ ,  $SCDF$  and  $SCDHF$ .
- If she travels from  $C$  to  $H$ , from  $H$  she must go to  $F$ . We have found another route,  $SCHF$ .
- If she travels from  $C$  to  $G$ , she must then go to  $H$  then  $F$ . We have found another route,  $SCGHF$ .

Therefore, there are five routes from  $S$  to  $F$  in which Jazzmin first travels from  $S$  to  $C$ . They are  $SCDEF$ ,  $SCDF$ ,  $SCDHF$ ,  $SCHF$ , and  $SCGHF$ .

In total, there are  $4 + 5 = 9$  different routes that Jazzmin can take from Entrance to Exit.

