## Problem of the Week Problem E and Solution <br> Coffee Sales

## Problem

For the months of April, May and June, Coffee Only sold coffee for $\$ 2.50$ per cup.
In May, they sold $y \%$ more cups of coffee than in April, where $y \geq 0$. In June, they sold $y \%$ fewer cups of coffee than in May.

Their records for sales in May were misplaced. They sold $\$ 31250$ worth of coffee in April. In June they sold $\$ 30800$ worth of coffee.

Determine the total value of the coffee they sold in May.

## Solution

Since the company had sales of $\$ 31250$ in April, the amount of coffee sold in April was $\frac{31250}{2.50}=12500$ cups.
Since the company had sales of $\$ 30800$ in June, the amount of coffee sold in June was $\frac{30800}{2.50}=12320$ cups.
In May, Coffee Only sold $y \%$ more cups of coffee than in April. In other words, they sold

$$
12500+12500\left(\frac{y}{100}\right)=12500\left(1+\frac{y}{100}\right)
$$

cups of coffee in May.
In June, they sold $y \%$ fewer cups of coffee than in May. In other words, they sold

$$
\left[12500\left(1+\frac{y}{100}\right)\right]-\left[12500\left(1+\frac{y}{100}\right)\right]\left(\frac{y}{100}\right)=\left[12500\left(1+\frac{y}{100}\right)\right]\left(1-\frac{y}{100}\right)
$$

cups of coffee in June.
We also know that Coffee Only sold 12320 cups of coffee in June. Therefore,

$$
\begin{aligned}
12500\left(1+\frac{y}{100}\right)\left(1-\frac{y}{100}\right) & =12320 \\
\left(1+\frac{y}{100}\right)\left(1-\frac{y}{100}\right) & =\frac{616}{625} \\
1-\frac{y^{2}}{10000} & =\frac{616}{625} \\
\frac{y^{2}}{10000} & =\frac{9}{625} \\
y^{2} & =144
\end{aligned}
$$

Since $y \geq 0$, we have $y=12$. Therefore, in May Coffee Only sold

$$
12500\left(1+\frac{y}{100}\right)=12500\left(1+\frac{12}{100}\right)=14000
$$

cups of coffee. The total value of the coffee sold in May was $14000 \times \$ 2.50=\$ 35000$.

